

## 2-Sided Tests and Confidence Intervals

In the 2000 NFL season, the home team won in 138 of 240 regular season games. Is this strong evidence that there is a different proportion of wins for home and away teams? Use  $\alpha = 0.05$ .

$$\hat{p} = \frac{138}{240}$$

- 1- What are the hypotheses?  
 $H_0: p = 0.50$   
 $H_a: p \neq 0.50$
- 2- What type of alternative hypothesis do we have (one or two sided)?  
two sided ( $\neq$ )
- 3- What is your significance level?  
 $\alpha = 0.05$
- 4- Do the full test of significance. Do you reject or fail to reject the null?

$$Z = \frac{\hat{p} - p}{\sqrt{\frac{p(1-p)}{n}}} = 2.324$$

p-value:



$$2 \cdot P(Z > 2.324) = 0.02$$

- reject

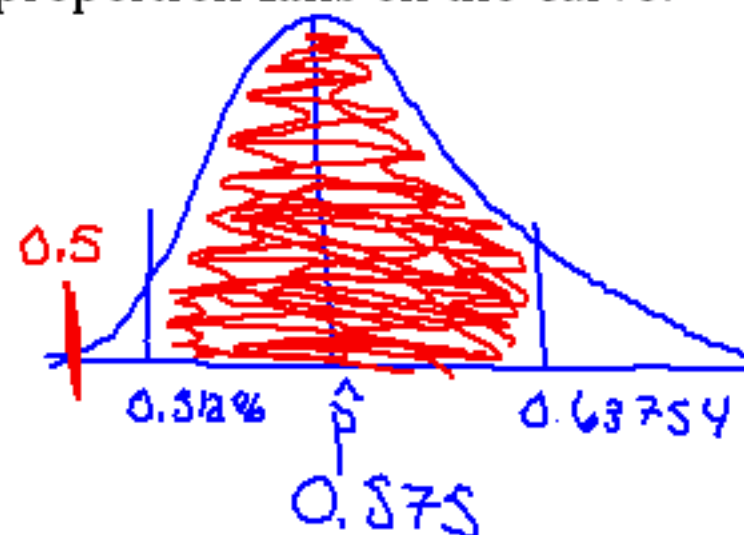
5- What is your sample proportion?  $\hat{p} = 0.575$

6- What is your claimed proportion (population proportion)?  $p = 0.5$

7- Create a 95% confidence interval for the proportion. (don't interpret, list interval below)

$(0.51246, 0.63754)$

8- Sketch a normal curve. Put your 95% confidence interval on this curve. Use your sample proportion as the center, since it's the center of your interval. Then mark where your claimed proportion falls on the curve.



9- Does your claimed proportion fall inside or outside of the interval? Did you reject this claim (the null) in your test of significance?

- outside  
- reject

## 2-Sided Tests and Confidence Intervals- Notes

- Confidence Intervals can also be used for...

2 sided tests

- The confidence level must "match" with...

$\alpha$  level

- Examples:

$$\alpha = 0.05 \Rightarrow \text{conf level } 95\%$$

$$\alpha = 0.03 \Rightarrow \text{conf level } 97\%$$

Steps for testing a claimed proportion (p) with a confidence interval:

1. Write hypothesis (must be  $\neq$ )

2. Determine  $\alpha$   $\Rightarrow$  Determine conf. level

3. Create conf. interval (a, b)

4. Look @ where  $\hat{p}$  falls (in or out)  
 $\nwarrow$  in  $H_0$

5. Determine Conclusion:

- Reject if... falls outside interval

- Fail to reject if... falls inside interval

6. Written Conclusion: at  $\alpha =$  claimed

- Reject/Fail to Reject because... the  $\hat{p}$  proportion falls outside/inside of the \_\_\_\_% conf. int.

- Sufficient evidence...  
same

$$\hat{p} \pm \text{margin of error}$$

### Examples:

1. A car service found that the emissions systems of 7 out of the 22 they tested failed to meet pollution control guidelines. Is this strong evidence against the claim that 20% of the fleet is out of compliance? Use a level of significance of 5%.

$$\hat{p} = \frac{7}{22} \quad \alpha = 0.05 \quad \text{CL} = 95\% \quad \text{Assump}$$

$$H_0: p = 0.20$$

$$H_a: p \neq 0.20$$

$$\hat{p} \pm z^* \sqrt{\frac{\hat{p}(1-\hat{p})}{n}} = (0.12355, 0.51281)$$

We fail to reject  $H_0$  @  $\alpha = 0.05$  b/c our claimed proportion falls w/in the 95% conf level

We have suff. evid that the prop of cars failing emissions is 20%

Try #2 and 3 on your own! - on board for E.C

For both #2 & 3:

(b) Using your confidence interval, what can be said about the actual value of the population proportion?  
(other than it's  $\neq$ )

- conf int.  $\rightarrow$  shows where true prop. lies.

same #2

$$\hat{p}_Y = \frac{7}{469}$$

$$\hat{p}_O = \frac{12}{500}$$

use conf. int.

$$\alpha = 0.05$$

$$H_0: p_Y = p_O \quad p_Y - p_O = 0$$

$$H_a: p_Y \neq p_O$$

$$(\hat{p}_Y - \hat{p}_O) \pm z^* \sqrt{\frac{\hat{p}_Y(1-\hat{p}_Y)}{n_Y} + \frac{\hat{p}_O(1-\hat{p}_O)}{n_O}}$$

$$= (-0.0264, 0.00826)$$

We fail to reject  $H_0$   
@  $\alpha = 0.05$  b/c 0 is in  
the 95% conf int.

